Physics - 8.01

Assignment #10

December 1, 1999.

It is strongly recommended that you read about a subject before it is covered in lectures.

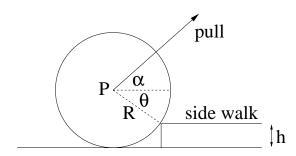
Lecture Date	Material Covered	Reading
#33 Fri 12/3	Kinetic Gas Theory - Ideal Gas Law PIVoT	Page 494 504
	Isothermal Atmosphere	Take Notes!
	Phase Diagrams - Phase Transitions	
#34 Mon 12/6	The Wonderful Quantum World Breakdown of Classical Mechanics	Take Notes!
#35 Wed 12/8		Bring a Friend

There is no due date for this assignment, and it will not be graded.

Solutions will be posted on Dec 10.

10.1 Lifting a Drum up the Sidewalk

A cylinder of mass M and radius R is lying on the street against the sidewalk. The height of the sidewalk is h. A rope is attached to the axis at each end (point P and Q) of the cylinder (we only show point P in the figure). We pull on the ropes (with equal force) perpendicular to the axis at an angle α with a horizontal plane so as to just lift the cylinder off the street.



- a) What is the ratio of this force (2 ropes combined) to the weight of the cylinder? Express your answer in terms of α , θ , M, and g.
- b) At what angle of α is the ratio as described under a) a minimum, and at what angle is it a maximum? Use $\theta = 30^{\circ}$.

10.2 Strain, Stress and Oscillations

A mass of 400 kg is hanging from a nylon rope of length 5 m and diameter 1 cm. We pull the mass down from its equilibrium position over a distance of 3 cm. (The stress is proportional to the strain.) Since the mass of the rope is much less than 400 kg you may neglect it.

- a) Calculate the force needed to do this.
- b) The mass is now released and it starts to oscillate vertically. Is the motion a SHO? What is the period of one oscillation?
- e) We now pull the mass down 10 cm from equilibrium and we release it. The stress is still proportional to the strain. Is the motion now a SHO?
- d) How much mass can we hang on the rope before it breaks? Any idea how long the rope then is?

10.3 Archimede's Principle

A uniform block of wood floats in water with two-thirds of its volume submerged. In oil it has 90% of its volume submerged. What is the density of the wood and of the oil?

Solutions for Assignment # 10

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December 8, 1999 9:54 am

Problem 10.1

(a) We pull with a force F (both ropes combined). At the point O the sidewalk exerts an unknown force F' on the cylinder. The condition for just lifting the cylinder off the street is N=0 where N is the usual normal force the street exerts on the cylinder. We can eliminate F' by measuring all torques about O. (A torque is defined as positive if it would cause the cylinder to roll up the sidewalk.) The condition for just rotating about the corner is $\tau=0$ where τ is the total torque about O.

$$0 = FR\sin(\pi - (\theta + \alpha)) - MgR\sin\left(\pi - \left(\frac{\pi}{2} - \theta\right)\right) = FR\sin(\theta + \alpha) - MgR\cos\theta$$

where we use the trigonometric identities $\sin(\pi - x) = \sin x$ and $\sin(\frac{\pi}{2} + x) = \cos x$. Solving the above equation for F gives

$$\frac{F}{Mg} = \frac{\cos \theta}{\sin(\theta + \alpha)}$$

(b) A local minimum or maximum occurs when

$$0 = \frac{dF}{d\alpha} = -Mg \cdot \frac{\cos\theta\cos(\theta + \alpha)}{\sin^2(\theta + \alpha)}$$

The only solution to the above equation is

$$\cos(\theta + \alpha) = 0 \implies \alpha = 90^{\circ} - \theta$$

For $\theta = 30^{\circ}$ then $\alpha = 60^{\circ}$. By plotting $\frac{F}{Mg}$ we see that $\alpha = 60^{\circ}$ is a local minimum and the global minimum and $\alpha = 0$ is the global maximum (not local). It's not hard to show that if $\theta < 45^{\circ}$ then the maximum is at $\alpha = 0^{\circ}$, and if $\theta > 45^{\circ}$ then the maximum is at $\alpha = 45^{\circ}$.