Cross Product, Torque, and Static Equilibrium

Generalization of Newton's Laws:

• External forces accelerate the center of mass

• External torques cause angular acceleration

Torque

Quantitative measure of the tendency of a force to cause or change the rotational motion of a body!

• (1) Magnitude of the torque about S

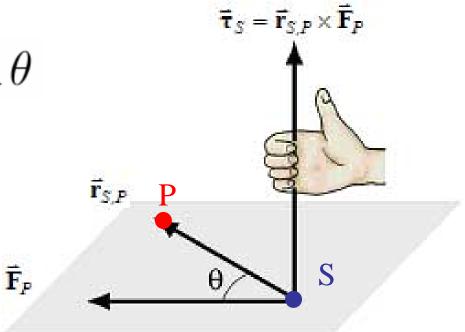
$$|\vec{\tau}_s| = |\vec{r}_{S,P}||\vec{F}_P|\sin\theta$$

• (2) Direction

$$\vec{\tau}_s = \vec{r}_{S,P} \times \vec{F}_P$$

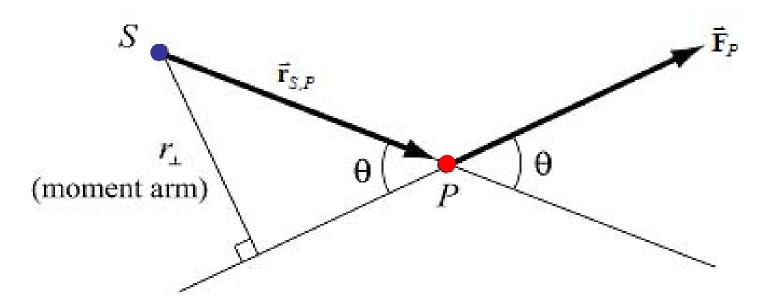
Sign convention:

Counterclockwise always positive!



Moment Arm of the Force

• Moment Arm:

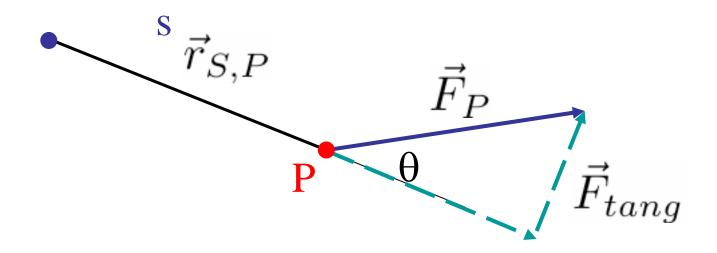


• Torque:

$$|\vec{\tau}_s| = +r_\perp |\vec{F}_P| = |\vec{r}_{S,P}| \sin \theta |\vec{F}_P|$$

Torque from Tangential Force

Break the force into components parallel and perpendicular to the displacement of the force from the axis of the torque:



$$|\vec{\tau}_s| = |\vec{r}_{S,P}||\vec{F}_{tang}| = |\vec{r}_{S,P}||\vec{F}_P|\sin\theta$$

Static Equilibrium

(1) The sum of the forces acting on the rigid body is zero:

$$\Sigma \vec{F} = 0$$

(2) The vector sum of the torques about any point S in a rigid body is zero:

$$\Sigma \vec{ au}_{ip} = 0$$

PRS Question

You are using a wrench to loosen a rusty nut. Which of the arrangements shown is most effective in loosening the nut?

