

➡ Last Lecture

- ➡ Pendulums and Kinetic Energy of rotation

➡ Today

- ➡ Energy and Momentum of rotation

➡ Important Concepts

- ➡ Equations for angular motion are mostly identical to those for linear motion with the names of the variables changed.
- ➡ Kinetic energy of rotation adds a new term to the same energy equation, it does not add a new equation.
- ➡ Momentum of rotation gives an additional equation

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Important Reminders

- ➡ Contact your tutor about session scheduling
- ➡ Mastering Physics due today at 10pm.
- ➡ Pset due this Friday at 11am.

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Torque Checklist

➡ Make a careful drawing showing **where** forces act

- ➡ Clearly indicate what axis you are using
- ➡ Clearly indicate whether CW or CCW is positive

➡ For each force:

- ➡ If force acts at axis or points to or away from axis, $\tau=0$
- ➡ Draw (imaginary) line from axis to point force acts. If distance and angle are clear from the geometry $\tau = Fr \sin(\theta)$
- ➡ Draw (imaginary) line parallel to the force. If distance from axis measured perpendicular to this line (lever arm) is clear, then the torque is the force times this distance

➡ Don't forget CW versus CCW, is the torque + or -

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Kinetic Energy with Rotation

➡ Adds a new term not a new equation!

- ➡ Rotation around any fixed pivot: $KE = \frac{1}{2} I_{pivot} \omega^2$

- ➡ Moving and rotating: $KE = \frac{1}{2} I_{CM} \omega^2 + \frac{1}{2} M_{Tot} v_{CM}^2$

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Everything you need to know for Linear & Rotational Dynamics

- $\Sigma \vec{F} = M\vec{a}$
- $\Sigma \vec{\tau} = I\vec{\alpha}$
 - This is true for **any fixed** axis and for an axis through the center of mass, even if the object moves or accelerates.
- Rolling **without** slipping: $v = R\omega$ $a = R\alpha$ $f \neq \mu N$
 - Friction does NOT do work!
- Rolling **with** slipping: $v \neq R\omega$ $a \neq R\alpha$ $f = \mu N$
 - Friction does work, usually negative.
 - Rarely solvable without using force and torque equations!

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Kinematics Variables

- | | |
|--------------------|---------------------------------|
| → Position x | → Angle θ |
| → Velocity v | → Angular velocity ω |
| → Acceleration a | → Angular acceleration α |
| → Force F | → Torque τ |
| → Mass M | → Moment of Inertia I |
| → Momentum p | → Angular Momentum $\vec{L}$ ❌ |

$$\omega = \frac{d\theta}{dt} \quad \alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$$

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Angular Momentum

- Conserved when external torques are zero or when you look over a very short period of time.
 - True for any fixed axis and for the center of mass
- Formula we will use is simple: $\vec{L} = I\vec{\omega}$
 - Vector nature (CW or CCW) is still important
- Point particle: $\vec{L} = \vec{r} \times \vec{p}$
- Conservation of angular momentum is a separate equation from conservation of linear momentum
- Angular impulse: $\vec{\tau} = \frac{d\vec{L}}{dt} \quad \Delta\vec{L} = \int \vec{\tau} dt$

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