Physics - 8.01

Assignment #2

September 15, 1999.

It is strongly recommended that you read about a subject before it is covered in lectures.

Lecture Date	Material Covered	Reading from Ohanian
#5 Fri 9/17	Circular Motion - Centrifuges	Page 84 86
	Perceived Gravity	
	Watch Videos on PIVoT (reference frames)	
#6 Mon 9/20	Newton's Laws	Page 99 112
#7 Wed 9/22	Weight - Perceived Gravity - Weightlessness	Page 123 134
	Free Fall - Zero-Gravity in Orbit (misnomer)	
	Watch Videos on PIVoT (weightlessness)	
#8 Fri 9/24	Friction There is an interesting article on	Page 134 140
,,	Friction in Scientific American, Oct, 1996.	3
	Watch Videos on PIVoT (friction)	
#9 Mon 9/27	Exam Review	Lectures #1 #5
Wed 9/29	Exam #1	Handout of 9/22

Due Friday, Sept 24, before 4 PM in 4-339B. Solutions will be posted on the Web Sat 9/25.

- 2.1 Throwing Stones page 51, problem 51.
- **2.2** Measurements of Gravitational Acceleration, g.

Use the measurements made during your first lecture of the two falling apples to calculate two values for g and their associated uncertainties. Do the two values agree within the accuracy of the measurements? Use the measurements obtained in the lecture that you attended.

2.3 Vector Addition page 70, problem 8.

Watch videos on PIVoT (under vector and look at the simulations).

- 2.4 Vectors page 71, problem 26.
- **2.5** Vector Scaling page 71, problem 27.
- **2.6** Keep in Touch with the Dutch.

Recently I drove in The Netherlands and I saw a road sign that indicated: Venlo 31 km, Eindhoven 39 km. Not knowing anything else, what is the minimum and what is the maximum distance (approximately) between these two towns.

2.7 Perpendicular Vectors.

The vectors $\mathbf{A} = 2\hat{\mathbf{x}} - 3\hat{\mathbf{y}}$ and $\mathbf{B} = -\hat{\mathbf{x}} + a\hat{\mathbf{y}} - 5\hat{\mathbf{z}}$ are perpendicular to each other. What is the value of a?

2.8 Adding, Subtracting, and Multiplication of Vectors—page 71, problem 25.

Watch videos on PIVoT (under vector and look at the simulations).

Calculate also:

$$d$$
) $A \cdot B$ and $B \cdot A$

e)
$$\mathbf{A} \times \mathbf{B}$$
 and $\mathbf{B} \times \mathbf{A}$

Problem 2.7

You are given the vectors

$$\vec{A} = 2\hat{x} - 3\hat{y}$$
 and $\vec{B} = -1\hat{x} + a\hat{y} - 5\hat{z}$

Now you must choose a value of a that makes \vec{A} and \vec{B} perpendicular. Mathematically you must satisfy

$$\overrightarrow{A} \cdot \overrightarrow{B} = 0$$

$$\Longrightarrow A_x B_x + A_y B_y + A_z B_z = 0$$

$$\Longrightarrow 2(-1) + (-3)(a) + 0(-5) = 0$$

$$a = -\frac{2}{3}$$

Problem 2.8

You are given the vectors

$$\vec{A} = -5\hat{x} - 3\hat{y} + \hat{z}$$
 and $\vec{B} = 2\hat{x} + 1\hat{y} - 3\hat{z}$

The calculations for parts (a), (b), and (c) are all done 'component-wise.'

$$\begin{array}{lll}
(\mathbf{a}) & \vec{A} + \vec{B} & = & (-5+2)\hat{x} + (-3+1)\hat{y} + (1+-3)\hat{z} \\
& = & -3\hat{x} - 2\hat{y} - 2\hat{z}
\end{array}$$

(b)
$$\vec{A} - \vec{B} = (-5 - 2)\hat{x} + (-3 - 1)\hat{y} + (1 - -3)\hat{z}$$

= $-7\hat{x} - 4\hat{y} + 4\hat{z}$

$$\begin{array}{lll} \textbf{(c)} & 2\vec{A} - 3\vec{B} & = & (2(-5) - 3(2))\hat{x} + (2(-3) - 3(1))\hat{y} + (2(1) - 3(-3))\hat{z} \\ & = & -16\hat{x} - 9\hat{y} + 11\hat{z} \end{array}$$

$$\begin{array}{rcl}
(\mathbf{d}) & \vec{A} \cdot \vec{B} &=& (-5)(2) + (-3)(1) + (1)(-3) \\
&=& -16
\end{array}$$

$$\vec{B} \cdot \vec{A} = (2)(-5) + (1)(-3) + (-3)(1)$$

= -16

In fact it is true that $\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}$ for any two vectors.

$$\begin{array}{lll}
(\mathbf{e}) & \vec{A} \times \vec{B} &= (-3)(-3) - (1)(1) \cdot \hat{x} + (-1)(2) - (-5)(-3) \cdot \hat{y} + (-5)(1) - (-3)(2) \cdot \hat{z} \\
&= 8\hat{x} - 13\hat{y} + 1\hat{z}
\end{array}$$

$$\vec{B} \times \vec{A} &= (-(1)(1) - (-3)(-3) \cdot \hat{x} + (-(-3)(-5) - (2)(1) \cdot \hat{y} + (-(2)(-3) - (1)(-5) \cdot \hat{z} \\
&= -8\hat{x} + 13\hat{y} - 1\hat{z} \\
&= -(8\hat{x} - 13\hat{y} + 1\hat{z})
\end{array}$$

In fact it is true that $\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$ for any two vectors.